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DPG-Tagung, Dortmund, March 31, 2006

- (quark)-flavor within SM and beyond: CKM and more
- rare processes: b -decays and mixing

CKM and CP → Klaus Schubert

rare decays → Manfred Paulini

B_s -mixing → Stephanie Menzemer

and many more in BSM, heavy quarks, rare decays sessions !

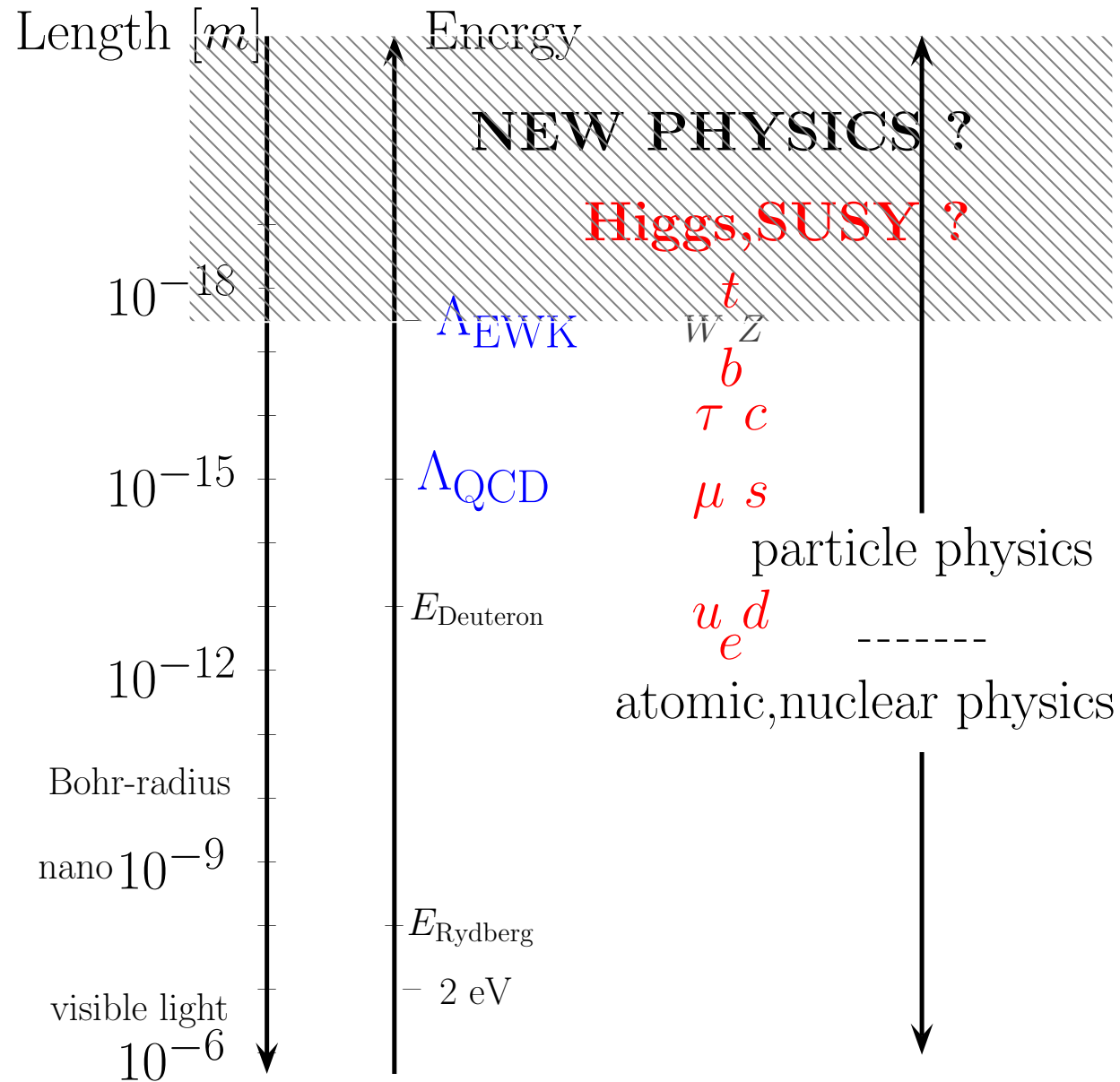
Core questions of flavor physics

- CP violation needed for baryogenesis $(n - \bar{n})/s \simeq 10^{-10}$
SM not sufficient
- strong CP problem: Why is $\bar{\Theta} \lesssim 10^{-10}$ and $\delta_{CKM} = \mathcal{O}(1)$?
- origin of flavor; explanation of peculiar masses and mixings
- neutrino masses

... are core questions of the SM, plus: unification, Higgs mass, dark matter, dark energy, gravity

despite its impressive experimental support the SM is rather viewed
as an effective theory valid up to $\Lambda \sim \mathcal{O}(m_W)$

The high energy frontier



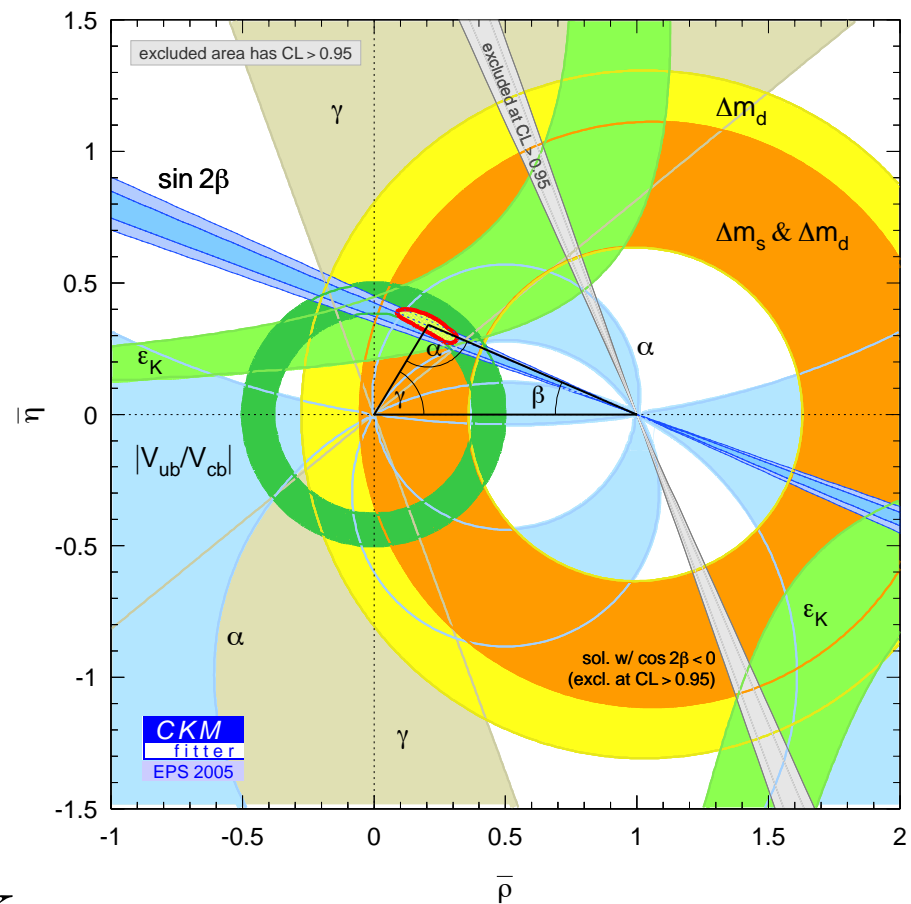
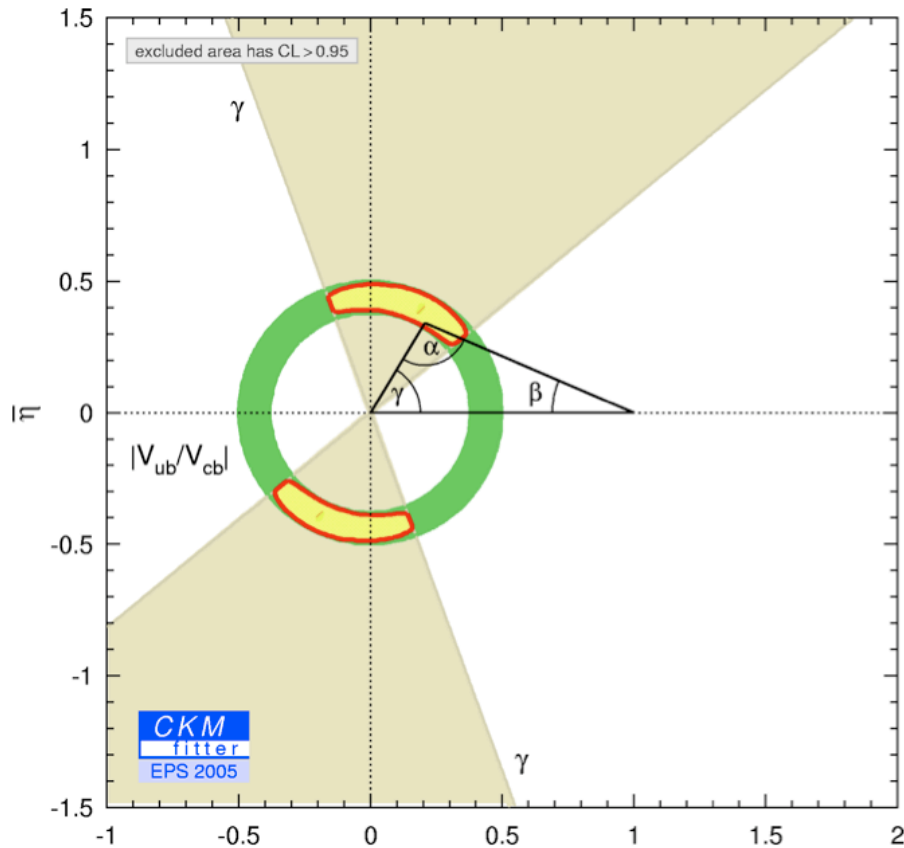
flavor and CP in SM: $-\mathcal{L}_Y = \bar{Q}Y_u h^c U + \bar{Q}Y_d h D + \bar{L}Y_e h E + h.c.$

flavor symmetry: $U(3)^5 \xrightarrow{Y} U(1)_B \times U(1)_L \times U(1)_Y$

quarks: $Y_{u,d}$ 36 real numbers \rightarrow 10 physical parameters: 6 quark masses plus CKM (3 angles, 1 phase)

- determine 10 parameters
- how do the Yukawas look like ? top-down, GUT's, textures, ED's, Froggatt-Nielsen, horizontal symmetries, anarchy, ..
- test the CKM-picture of flavor/CP violation, that is, **MFV**
minimal flavor violation = no further breaking of flavor than through Yukawas
- are there deviations from the SM in rare processes ?

CKM 2005: unitarity triangle from tree level, precision



tree fit with V_{ub} , $\gamma^{\bar{p}}$ from $B \rightarrow DK$

loop input to full fit: meson mixing, $\sin 2\beta(\bar{c}c)_{data-ave} = 0.687 \pm 0.032$

SM/MFV-like picture at least for $b \rightarrow \bar{c}cs$, K -, B_d -mixing

CKM=precision input within MFV $\epsilon(\alpha) = 6\%$, $\epsilon(\beta) = 4\%$, $\epsilon(\gamma) = 10\%$

SM tests with indirect processes

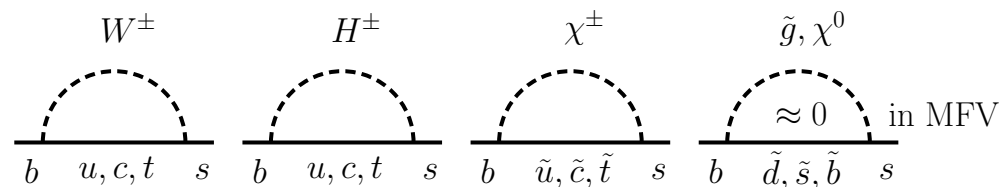
indirect loop processes:

$\Lambda \gtrsim m_W$ scale of New Physics

$$\mathcal{L}_{eff} = \sum_i c_i^{(n)} \frac{O_i^{(n)}}{\Lambda^n} \quad c_i^{(n)} \leftrightarrow f\left(\underbrace{m_j, g_l, \dots}_{colliders}; \underbrace{\varphi_{CKM}, \varphi_m, \delta_n}_{flavorphysics}\right)$$

no competition from large SM tree contributions

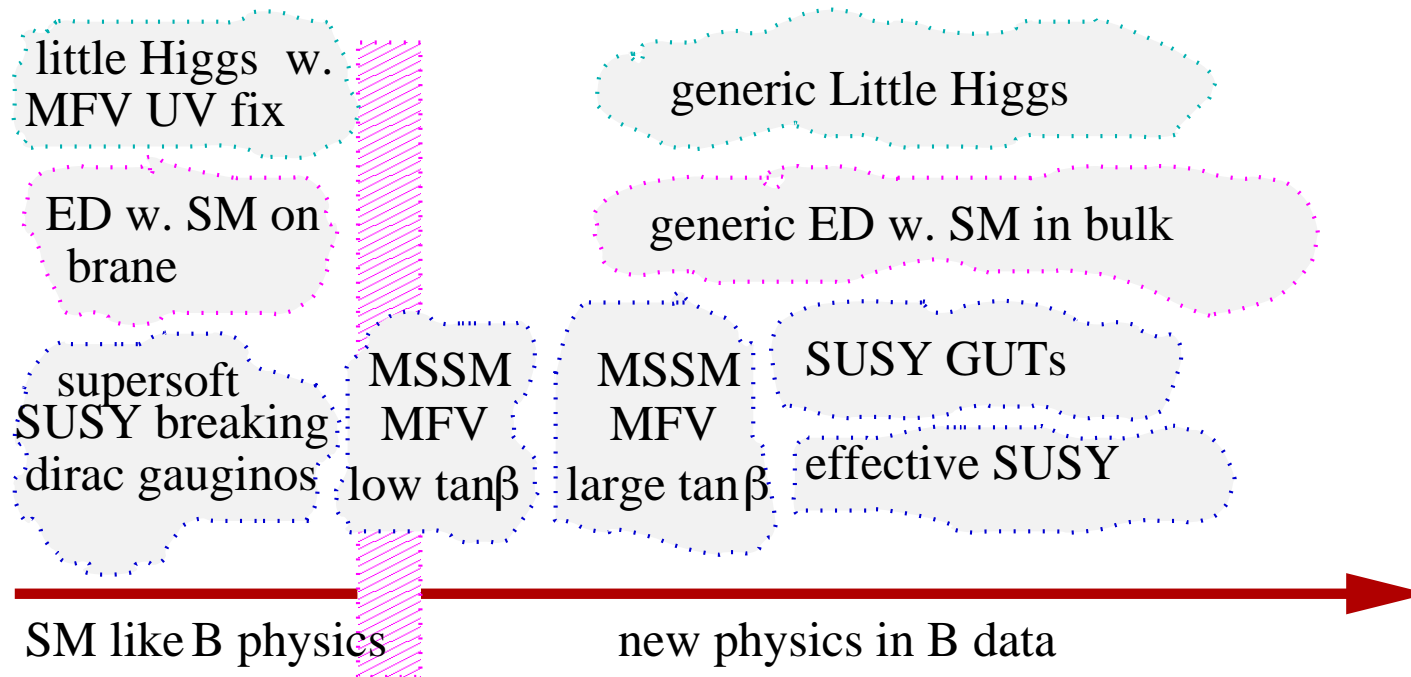
FCNC: sensitivity to SM, NP phases φ , flavor-breaking couplings δ



BSM contributions to FCNC can offset rates, distort spectra, induce CP-asymmetries, V+A currents

models of EWKSB with NP @ TeV

Fig from hep-ph/0207121



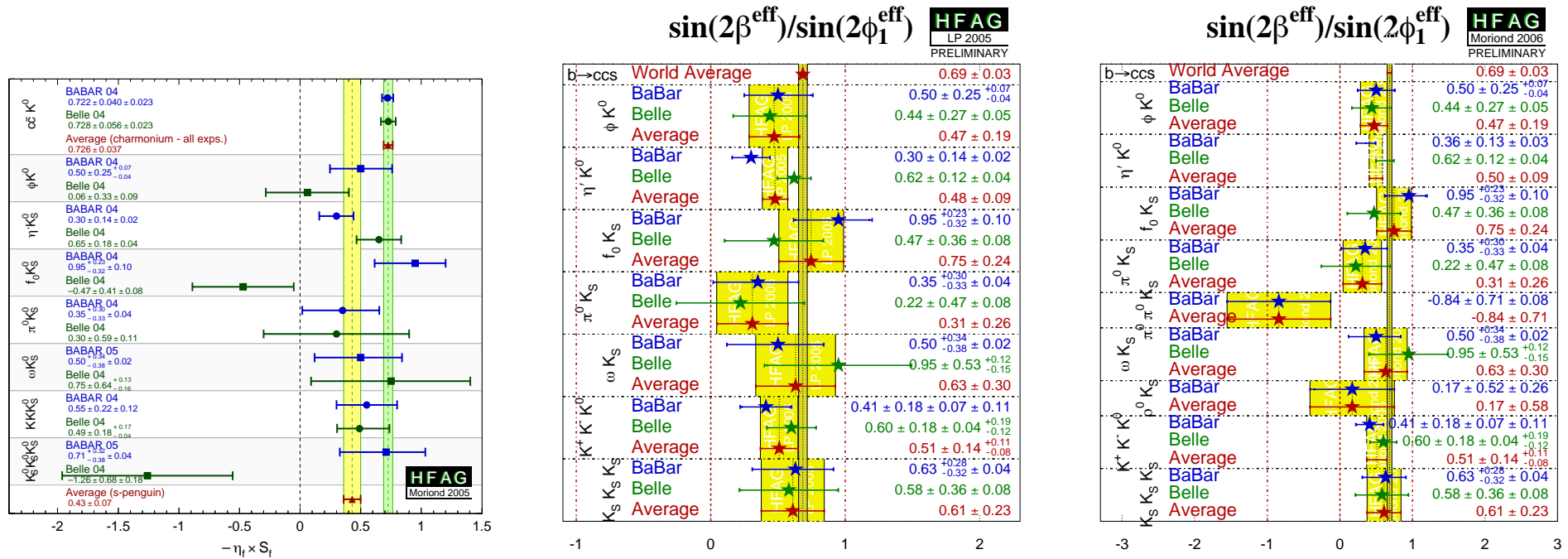
reach in indirect signals rare b, c, K, τ -decays, mixing, EDMs, $g-2$
depends on beyond the SM flavor/CP violation (minimal=CKM ?),
large parameters e.g. $\tan\beta$ and theor. and exp. uncertainties

- searching for BSM CP-violation in $b \rightarrow s$ penguins
- today's and future impact of $b \rightarrow s\ell\ell$ modes
- $B_s - \bar{B}_s$ mixing

Time-dependent CP asymmetries in $b \rightarrow s\bar{q}q$ decays

$$\text{SM+MFV: } -\eta_{CP} \sin 2\beta \underbrace{\left((\bar{s}s) K_S \right)}_{FCNC} = \sin 2\beta \underbrace{\left((\bar{c}c) K_S \right)}_{tree} + \underbrace{\left| \frac{V_{ub}V_{us}^*}{V_{tb}V_{ts}^*} \right|}_{\mathcal{O}(\lambda^2)} \cdot \#$$

SM background $\mathcal{O}(\lambda^2) \sim 0.04$, $\#$ non-universal, hadronic physics



since Moriond05: $\sim 1\sigma$ shifts in $\bar{c}c$, Φ , larger ones K_S^3 , f_0 ; η' off by 2.3σ
 better agreement between Belle and BaBar; new 2006: ρK_S (BaBar)

$$\Delta S = -\eta_f S_f - \sin 2\beta$$

hep-ph/0505075, 0503151 hep-ph/9708305, 0310020, 0303171, 0403287

f	$\Delta S_{SM}^{QCDF@NLO}$	$\Delta S_{SM}^{QCDF@LO}$	$ \Delta S_{SM}^{SU(3)+} $	S_f LP'05	C_f LP'05
ΦK^0	0.01 ... 0.03	0.02	$\lesssim 0.3$	0.47 ± 0.19	-0.09 ± 0.14
$\eta' K^0$	0 ... 0.02	-0.01 ... 0.02	$\lesssim 0.15$	0.48 ± 0.09	-0.08 ± 0.07
$\pi^0 K_S$	0.03 ... 0.12	0.03 ... 0.10	$\lesssim 0.2$	0.31 ± 0.26	-0.02 ± 0.13
ωK_S	0.05 ... 0.22	0.05 ... 0.25	—	0.63 ± 0.30	-0.44 ± 0.23

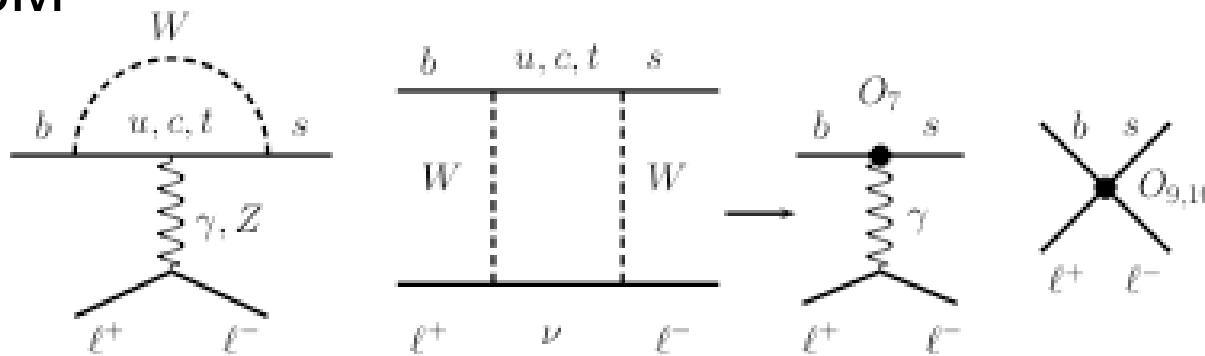
LO captures central value and uncertainty of full NLO calc. of ΔS_f

for all above modes: QCD factorization predicts $\Delta S_f > 0$,
 experimental shifts < 0 ; no significant $C_f \neq 0$

ultimately more precision needed; all exp. errors $\lesssim 0.1$ only by time of
 super- b -factory hep-ph/0503261; ηK_S data missing

SM tests with $b \rightarrow s\gamma, b \rightarrow sl^+\ell^-$ decays

diagrams in SM



$$\mathcal{H}_{\text{eff}} = -4 \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum C_i(\mu) O_i(\mu)$$

dipole operators $O_7 \propto \bar{s}_L \sigma_{\mu\nu} b_R F^{\mu\nu}$

$O_8 \propto \bar{s}_L \sigma_{\mu\nu} b_R G^{\mu\nu}$

4-Fermi operators $O_9 \propto (\bar{s}_L \gamma_\mu b_L)(\bar{\ell} \gamma^\mu \ell)$

$O_{10} \propto (\bar{s}_L \gamma_\mu b_L)(\bar{\ell} \gamma^\mu \gamma_5 \ell)$

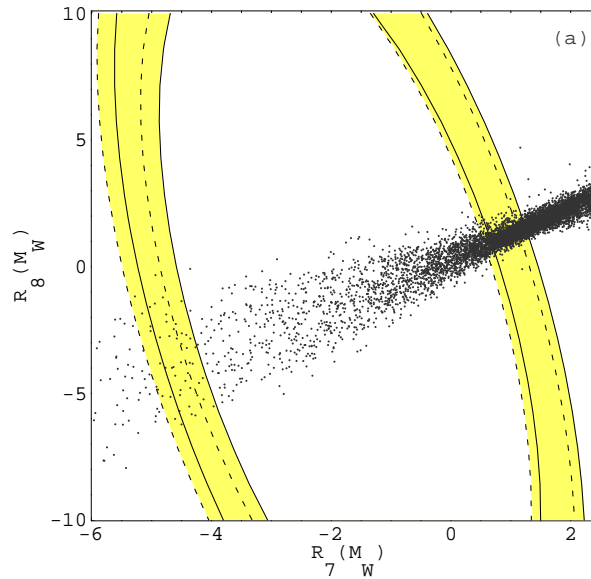
NP in Wilson coefficients $C_i = C_i^{SM} + C_i^{NP}$ or new operators

model-independent analysis: Br 's, $A_{CP}, A_{FB} = f(C_i) \rightarrow \text{fit!}$ [hep-ph/9408213](https://arxiv.org/abs/hep-ph/9408213)

Constraints from $b \rightarrow s\gamma$ branching ratio

$$\mathcal{B}(b \rightarrow s\gamma)_{LO} \sim |C_7(m_b)|^2 \quad \text{at NLO } R \equiv \frac{C^{SM} + C^{NP}}{C^{SM}} \quad \text{hep-ph/0112300}$$

$$R_8 - R_7:$$



theory errors renorm. scale and charm mass **solid:pole, dashed:MS**

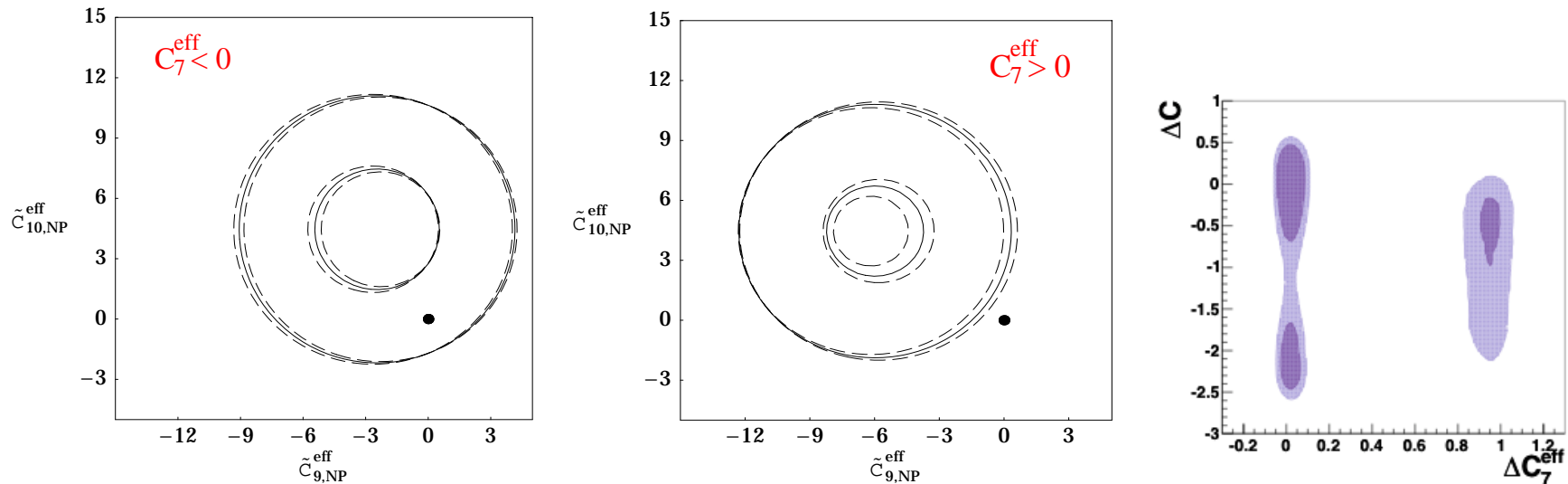
scatter points: MSSM with MFV: $C_7 = \underbrace{C_7^{SM} + C_7^{H^\pm}}_{<0} + C_7^{\chi^\pm}$

$C_7^{\chi^\pm} \propto \mu A_t \tan \beta f(m_{\tilde{t}_i}, m_{\tilde{\chi}_j}) m_b / (v(1 + \epsilon \tan \beta)); \epsilon \propto (\alpha_s/\pi) \mu m_{\tilde{g}} \tan \beta$

beyond MFV: gluino loops with down squark-mixing δ_{23}^D e.g. hep-ph/0212397

Combined $b \rightarrow sl^+l^-$ and $b \rightarrow s\gamma$ data

$$\frac{d\Gamma(B \rightarrow X_s l^+ l^-)}{d\hat{s}} = \left(\frac{\alpha}{4\pi}\right)^2 \frac{G_F^2 m_b^5 |V_{ts}^* V_{tb}|^2}{48\pi^3} (1 - \hat{s})^2 \left[(1 + 2\hat{s}) \left(|C_9^{\text{eff}}|^2 + |C_{10}^{\text{eff}}|^2 \right) f_1 \right. \\ \left. + 4(1 + 2/\hat{s}) |C_7^{\text{eff}}|^2 f_2 + 12\text{Re} \left(C_7^{\text{eff}} C_9^{\text{eff}*} \right) f_3 + f_c \right] \quad f_i: 1/m_{c,b}^2 \text{ corr.}$$



non-SM sign $C_7^{\text{eff}} > 0$ disfavored iff no BSM ops [hep-ph/0410155, 0505110\(C10-C7study\)](#)

MSSM+MFV: C_9, C_{10} near SM, not $\tan\beta$ enhanced [hep-ph/0112300](#)

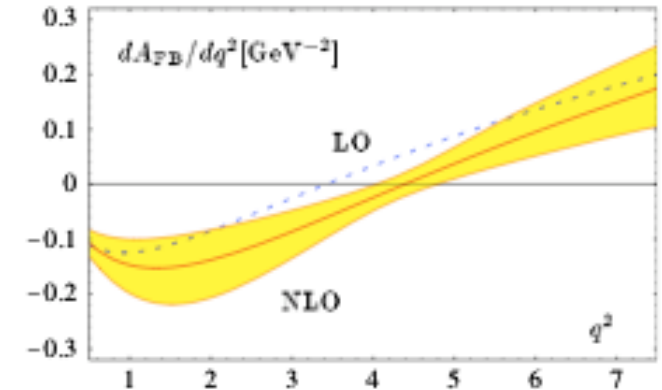
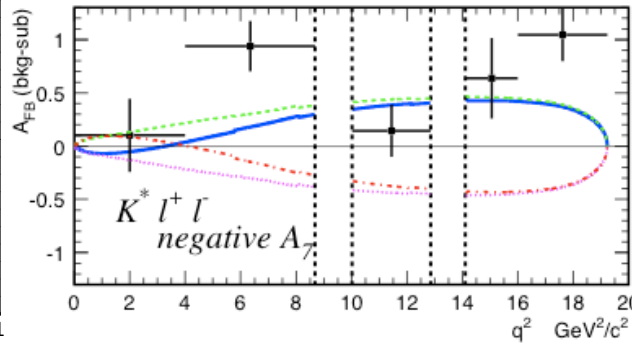
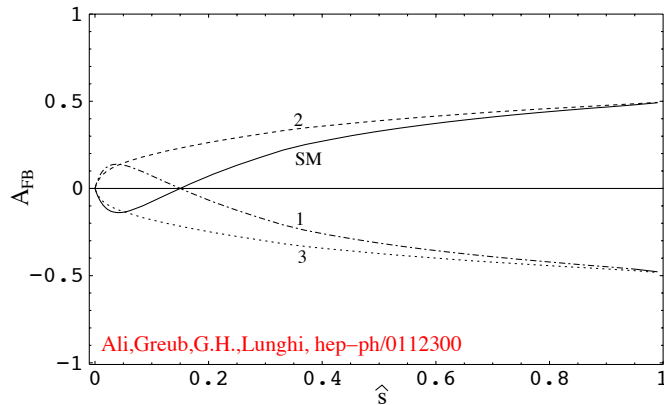
neutral Higgs effects $O_{S(P)}^f \sim \bar{s}_L b_R \bar{f} (\gamma_5) f$, $\tan\beta$ enhanced

check for BSM operators *i* (pseudo)scalar *ii* $L \leftrightarrow R$ flipped O'_i *iii* ..

NP sensitivity of $b \rightarrow sl^+l^-$ spectra, perspectives

A_{FB} : # forward - # backward l^+ in dilepton CMS w.r.t. \bar{B} (CP-odd)

$A_{FB}(\hat{s}) \sim \text{Re} [C_{10}^*(C_7^{\text{eff}} + \beta(\hat{s})C_9^{\text{eff}})]$ also $B \rightarrow K^*l^+l^-$ Belle 0508009,0603018



shape sensitive to sign C_7 ; $A_{FB} \propto C_{10}$; flat possible

zero X_S : $\hat{s}_{SM}^{NNLL} = 0.162 \pm 0.002(8)$ hep-ph/0208088,0209006

K^* : $s_{SM}^{NLO} = 4.4 \pm 0.4 \text{ GeV}^2$ hep-ph/0106067

CP $A_{FB}^{CP} \equiv \frac{A_{FB} + \bar{A}_{FB}}{A_{FB} - \bar{A}_{FB}} \sim \arg C_{10} \arg C_9^{\text{eff}} ; A_{FB}^{CP}|_{SM} \lesssim 10^{-3}$ hep-ph/0006136

full angular analysis $B \rightarrow K^*(\rightarrow K\pi)l^+l^-$ hep-ph/9907386

$$d\Gamma^4 \sim I(s, \Theta_l, \Theta_{K^*}, \Phi) ds d\cos\Theta_l d\cos\Theta_{K^*} d\Phi$$

More model-independent studies, neutral Higgses

Higgses split between $\mu^+\mu^-$ and e^+e^- in $b \rightarrow sl^+\ell^-$ ratios with SAME cut on dilepton mass hep-ph/0310219

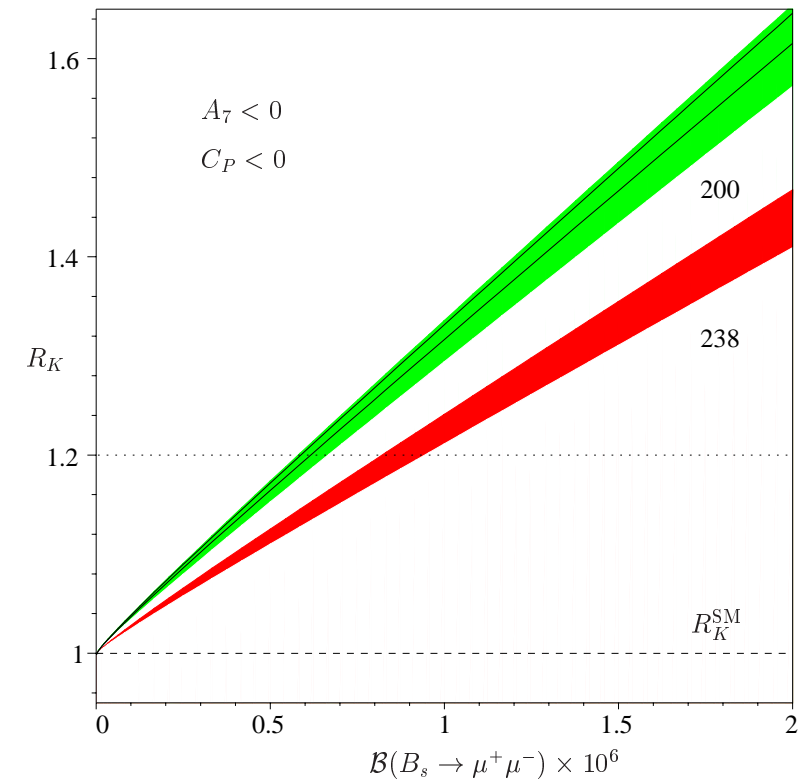
$$R_H \equiv \frac{\int_{4m_\mu^2}^{q_{\max}^2} dq^2 \frac{d\Gamma(B \rightarrow H\mu^+\mu^-)}{dq^2}}{\int_{4m_\mu^2}^{q_{\max}^2} dq^2 \frac{d\Gamma(B \rightarrow He^+e^-)}{dq^2}} \quad H = X_s, K^{(*)}$$

$$R_H^{SM} = 1 + \mathcal{O}(m_\mu^2/m_b^2) \quad \text{very clean}$$

$$R_K = 1.06 \pm 0.48 \pm 0.05 \quad \text{BaBar 0507005}$$

$$R_K = 1.38_{-0.41-0.07}^{+0.39+0.06} \quad \text{Belle 0410006}$$

constrain (pseudo)-scalar couplings



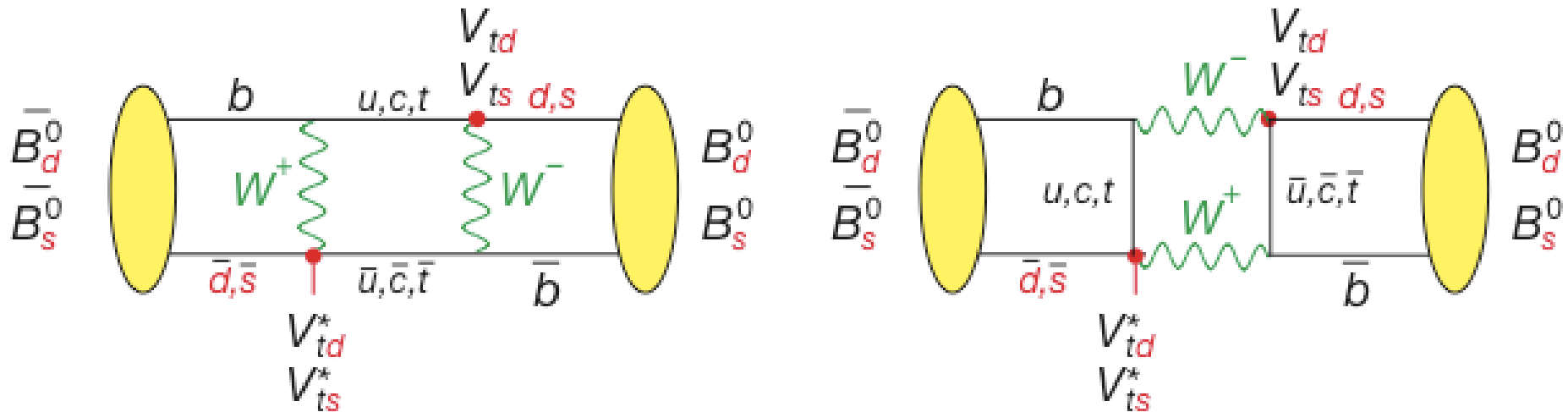
R_K constrains $C_{S,P} + C'_{S,P}$, $\mathcal{B}(B_s \rightarrow \mu^+\mu^-)$ constrains $C_{S,P} - C'_{S,P}$
correlation breaks down if $C_{S,P} \not\propto m_\ell$

a theoretical exercise

*DØ: $17 < \Delta m_s < 21 \text{ ps}^{-1}$ at 90% C.L. hep-ex/0603029

SM: $W - (u, c, t)$ -box $\Delta m_s^{\text{SM}} \sim (V_{tb}^* V_{ts})^2 \frac{g^4}{16\pi^2} \frac{(\bar{b}\Gamma_s)(\bar{b}\Gamma'_s)}{m_W^2}$

top dominated; $V_{tb} \simeq 1$, $V_{ts} = -A\lambda^2$ independent of CKM-triangle-fit



$$\Delta m_d^{\text{world ave}} = 0.570 \pm 0.004 \text{ ps}^{-1} \text{ (HFAG '05)}$$

$$\Delta m_s^{\text{SM}} = 18.3_{-1.5}^{+6.5} \text{ ps}^{-1} \text{ (CKMfitter/EPs'05)} \quad \Delta m_s^{\text{SM}} = 20.0 \pm 1.8 \text{ ps}^{-1} \text{ (UTfit hep-ph/0501199)}$$

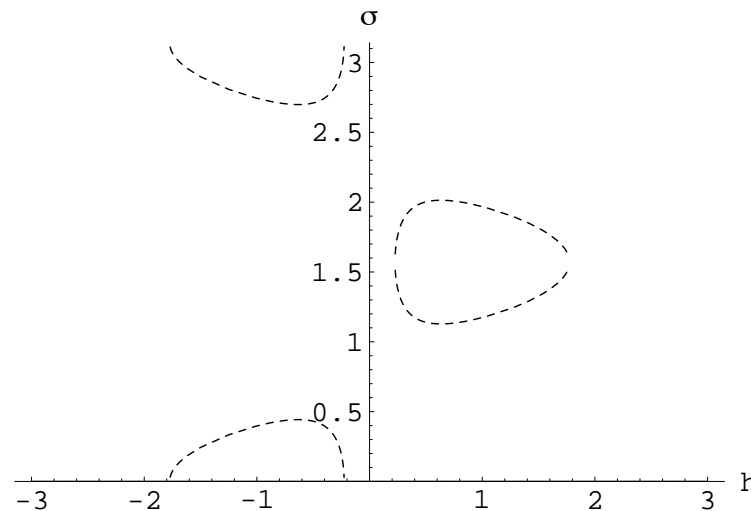
assume in plots: $\Delta m_s^{\text{SM}} = \Delta m_s^{\text{data}} = 19.0 \pm 2 \text{ ps}^{-1} @ 90 \% \text{ C.L.}$

generic NP constraints from lower bound

mixing with NP: $\Delta m_s = \Delta m_s^{\text{SM}} \cdot |1 + h e^{2i\sigma}|$ see also hep-ph/0509117 for nicer plots

only lower bound near SM $\Delta m_s > 16.6 \text{ ps}^{-1}$ @ 95 % C.L. (HFAG '05)

$\Delta m_s > \Delta m_s^{\text{SM}}(1 - \epsilon)$:



dotted: $\epsilon = 0.23$

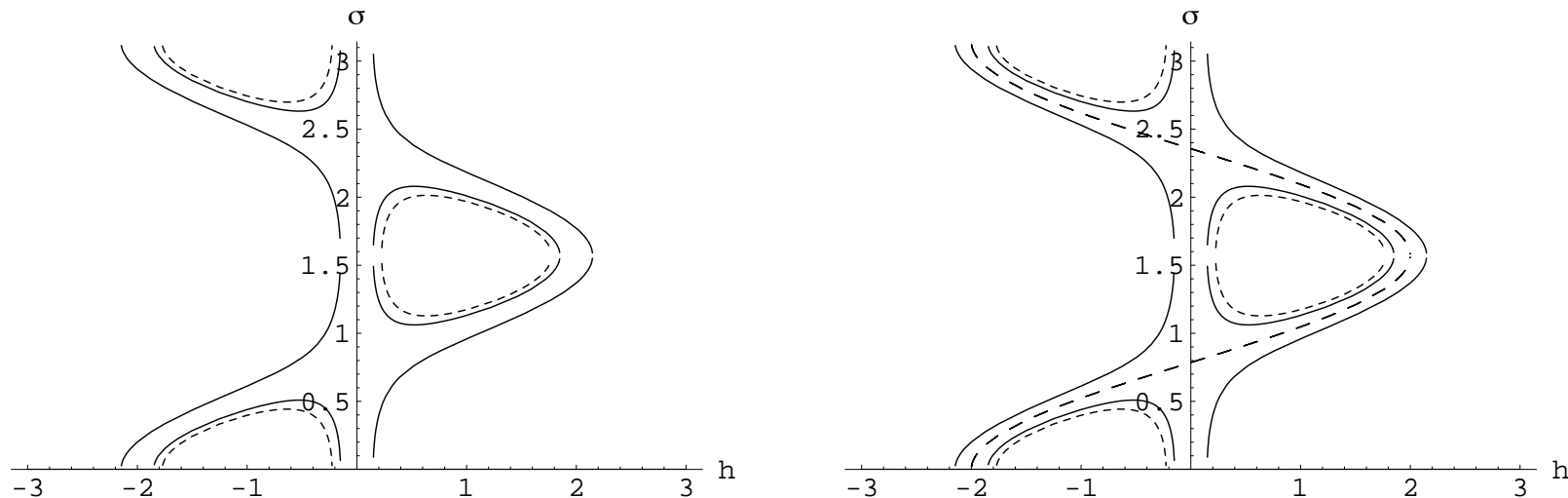
gaps excluded around $h \simeq +1, \sigma \simeq \pi/2$ and $h \simeq -1$ with $\sigma \simeq 0, \pi$

size of NP-amplitude h unconstrained

generic NP constraints: measurement

$$\Delta m_s = \Delta m_s^{\text{SM}} \cdot |1 + h e^{2i\sigma}|; \text{ with } \Delta m_s \simeq \Delta m_s^{\text{SM}} (1 \pm \epsilon)$$

$$\Delta m_s^{\text{data}} = 19.0 \pm 2 \text{ ps}^{-1} \text{ @ 90 \% C.L.}$$



dotted: lower bound only, solid: $\epsilon = 0.15$, dashed (and $h = 0$): $\epsilon = 0$

size of NP-amplitude $|h| < 2 + \epsilon$ limited

$\mathcal{O}(1)$ NP-amplitude possible if NP-phase σ cooperates

large $|h|$ is fine-tuned to some degree for small errors $\epsilon \rightarrow 0$

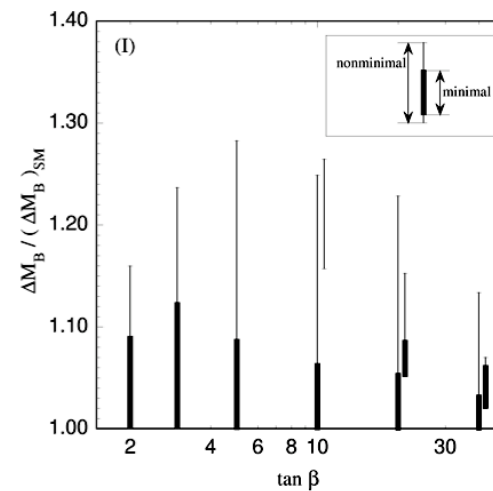
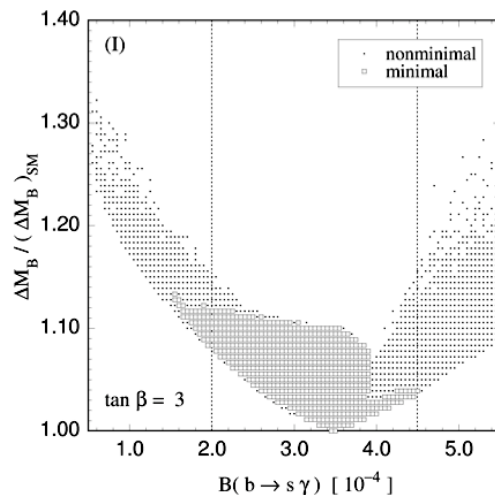
I. low $\tan \beta$: CKM-ology: hep-ph/9903535, SUGRA: hep-ph/9908499

$h = h_{H^\pm} + h_{\chi^\pm}$; $\sigma = 0$ (no BSM CP-violation)

$h > 0$ in whole parameter space h equal for B_d and B_s

ok with $b \rightarrow s\gamma$, $m_\chi > 91$ GeV, all other charged SUSY-partners above 80 GeV: $0 < h \lesssim 0.75$; h decreases for heavy $m_{\tilde{t}}, m_{\tilde{\chi}}, m_{H^\pm}$

SUGRA: $h \lesssim 0.4$; calc. only valid up to moderate $\tan \beta$ (see next slide)

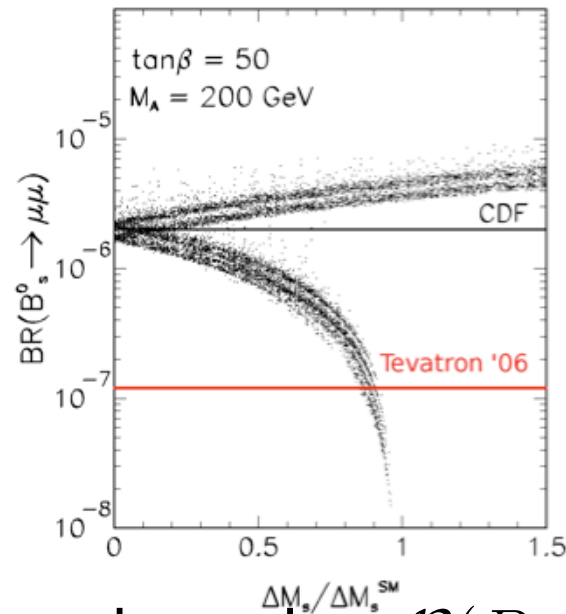


II. large $\tan \beta$: [hep-ph/0210145](#) $h = \underbrace{h_{H^\pm}}_{<0} + \underbrace{h_{\chi^\pm}}_{>0} + \underbrace{h_{DP}}_{<0}, \sigma = 0$

$h < 0$ in most of the parameter space; $h(B_d) \neq h(B_s)$ due to DP

DP: double penguin from neutral Higgses: $DP(B_s) \propto m_s \tan \beta^4$ big!

Δm_s correlated with $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 1.2 \cdot 10^{-7}$ [hep-ph/0207241](#)



lower bound on Δm_s predicts upper bound on $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$

$W = QY_u H_u U + QY_d H_d D + LY_e H_d E + \lambda H_d H_u N - \frac{1}{3}kN^3$ N :singlet
at large $\tan \beta$: naturally light pseudoscalar A_1^0 , radiatively stable

A_1^0 masses as low as $\mathcal{O}(10\text{MeV})$ viable [hep-ph/0404220](#)

iff very light and weakly coupled, A_1^0 becomes missing E

$h^0 \rightarrow A^0 A^0$ very important for Higgs searches [hep-ph/0005308](#)

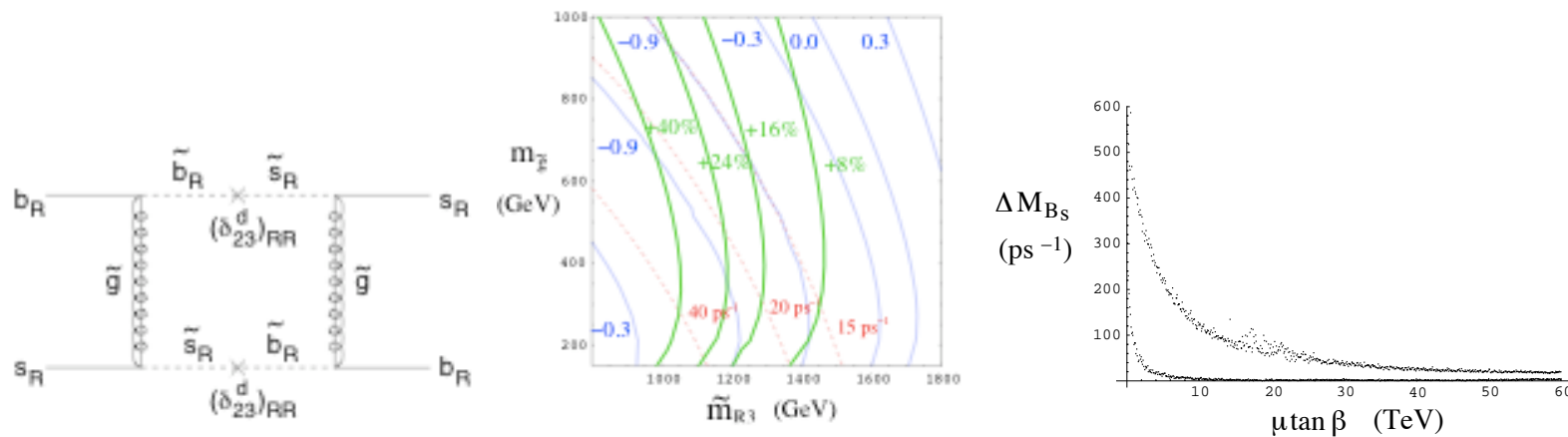
NMSSM at large $\tan \beta$: $h = h_{MSSM}^{large \tan \beta} + h_{A_1^0}$; $h_{A_1^0} \propto \tan \beta^2 / m_{A_1^0}^2$

$$h_{A_1^0}(B_d) = h_{A_1^0}(B_s)$$

from Δm_d -measurement: $|h| \lesssim 0.4$

unlike MSSM, no correlation with $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$ [hep-ph/0404220](#)

large $\nu_\mu - \nu_\tau$ mixing in $SO(10)$ GUT models implies large mixing between right handed $\tilde{s} - \tilde{b}$: $(\delta_{23}^D)_{RR}$ large and complex Figs from hep-ph/0212180



implications: Δm_s can be huge $\sim 100 \text{ ps}^{-1}$ (range in right fig) but can be also SM-like (middle fig):

needs heavy superpartners $m_{Q2,Q3,D2} \sim 2\text{TeV}$
or small couplings $(\delta_{23}^D)_{RR}$

(green: percent increase in $B(b \rightarrow s\gamma)$, blue: $S_{\Phi K_S}$)

- CKM@tree: input for SM tests and flavor model building thanks to tremendous exp and th (loops, HQET, lattice, ..) efforts
- in 2005 $\sin 2\beta_{\text{penguin}}$ moved closer to MFV, some hints $\eta' K^0$
- $b \rightarrow s\ell\ell$ modes under th and exp investigation; model independent analysis (w. $b \rightarrow s\gamma$) \rightarrow do e and μ separately long term goal: angular analysis in $B \rightarrow K^*(\rightarrow K\pi)\ell\ell$
- tool in penguin-physics: **multi-observable analyses and fits**
- $b \rightarrow d$ FCNCs beginning to be probed
- B_s, B_c, Λ_b -physics coming up CDF&D0; much more from LHC(b)

- an upper bound on $B_s - \bar{B}_s$ mixing touches unknown territory
IFF $\Delta m_s \simeq \Delta m_s^{\text{SM}}$
- generically, $O(1)$ NP allowed with some amount of fine-tuning and CP-phase; further constrains from $\Delta\Gamma$ and CP-asymmetries
- models with MFV, such as CMSSM can accommodate SM-like $B_s - \bar{B}_s$ -mixing within errors $|h| < \epsilon$
- models beyond MFV are constrained by this significantly
- $|V_{td}/V_{ts}|_{\text{treeUT}}$ vs $|V_{td}/V_{ts}|$ from $\frac{\Delta m_d}{\Delta m_s} = \left| \frac{V_{td}}{V_{ts}} \right|^2 \xi^{-2} \frac{m_{B_d}}{m_{B_s}}$: SM test !
- so far no significant conflict with SM/MFV; many FCNCs only weakly or just un-constrained $V + A, \tau^\pm, \nu\bar{\nu}, b \rightarrow d, B_s$ -physics

Some (further) SM tests with b -physics

	experiment	SM	comments
$a_{CP}(b \rightarrow s\gamma)$	$0.4 \pm 3.6 \%$	$0.42 \pm 0.17 \%$ <small>hep-ph/0312260</small>	CPX in $bs\gamma, g$
$a_{CP}(b \rightarrow d/s\gamma)$	-0.110 ± 0.116 <small>BaBar'05</small>	10^{-9} <small>hep-ph/0312260</small>	test MFV
$S_{K_S\pi^0\gamma}$	0.00 ± 0.28 <small>Belle/BaBar'05</small>	$-2m_s/m_b$	V+A FCNCs
spin $\Lambda_b \rightarrow \Lambda\gamma$	–	$\sim m_s/m_b$	V+A FCNCs
$\mathcal{B}(B \rightarrow X_s g)$	$< 9\%$ <small>CLEO'97</small>	$5.0 \pm 1.0 \cdot 10^{-3}$	NP in bsg
TDCPA $b \rightarrow s\bar{s}s$	$S_{ave} = 0.50 \pm 0.06$	$\sin 2\beta + \Delta S$	CPX
$\mathcal{B}(B \rightarrow X_s \bar{\mu}\mu)$	$4.3 \pm 1.2 \cdot 10^{-6}$	$4.3 \pm 0.7 \cdot 10^{-6}$	q^2 -spectra
$a_{CP}(B \rightarrow X_s \bar{\ell}\ell)$	-0.22 ± 0.26	$-0.2 \pm 0.2 \%$ <small>hep-ph/9812267</small>	CPX
$A_{FB}^{CP}(B \rightarrow K^* \bar{\ell}\ell)$	–	$\lesssim 10^{-3}$ <small>hep-ph/0006136</small>	CPX in bsZ
$R_K \mu\mu$ vs. ee	1.06 ± 0.48 <small>BaBar'05</small>	$1 + \mathcal{O}(m_\mu^2/m_b^2)$ <small>hep-ph/0310219</small>	non-SM Higgs
$\mathcal{B}(B \rightarrow K\nu\bar{\nu})$	$< 3.6 \cdot 10^{-5}$ <small>Belle'05</small>	$3.8_{-0.6}^{+1.2} \cdot 10^{-6}$	$O(10)$ from SM
$\mathcal{B}(B_s \rightarrow \mu^+\mu^-)$	$< 1.2 \cdot 10^{-7}$	$3.2 \pm 1.5 \cdot 10^{-9}$	$O(50)$ from SM
$\mathcal{B}(B_s \rightarrow \tau^+\tau^-)$	$< \mathcal{O}(5\%)$	$7.2 \pm 1.1 \cdot 10^{-7}$	$O(10^5)$ from SM
$\mathcal{B}(B_d \rightarrow \tau^+\tau^-)$	$< 3.4 \cdot 10^{-3}$ <small>BaBar'05</small>	$2.1 \pm 0.3 \cdot 10^{-8}$	$O(10^5)$ from SM

order 1 NP on $\Delta m_s^{\text{SM}} \sim (V_{tb}^* V_{ts})^2 \frac{g^4}{16\pi^2} \frac{(\bar{b}\Gamma_s)(\bar{b}\Gamma'_s)}{m_W^2}$ implies

	NP from loops	tree level NP
MFV	$\Lambda \gtrsim m_W \sim O(100) \text{ GeV}$	$\Lambda \gtrsim 4\pi m_W \sim O(1) \text{ TeV}$
non MFV	$\Lambda \gtrsim m_W / V_{ts} \sim O(2 - 3) \text{ TeV}$	$\Lambda \gtrsim 4\pi m_W / V_{ts} \sim O(30) \text{ TeV}$

origin of flavor is still a mystery

whether it is connected to the NP scale Λ we are probing now